COOLING WATER SYSTEMS DESIGN USING PROCESS INTEGRATION

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ABSTRACT
Cooling water systems are generally designed with a set of heat exchangers arranged in parallel. This arrangement results in higher cooling water flowrate and low cooling water return temperature thus reducing cooling tower efficiency. Previous research on cooling water systems has focused mainly on heat exchanger network thus excluding the interaction between heat exchanger network and the cooling towers. This manuscript presents a technique for grassroot design of cooling water system for wastewater minimization which incorporates the performances of the cooling towers involved. The study focuses mainly on cooling systems consisting of multiple cooling towers that supply a common set of heat exchangers. The heat exchanger network is synthesized using the mathematical optimization technique. This technique is based on superstructure in which all opportunities for cooling water reuse are explored. The cooling tower model is used to predict the thermal performance of the cooling towers.

KEY WORDS
Mathematical optimization; Cooling water system; Cooling tower; Heat exchanger network

1. Introduction
Industrial development and other economic activities have led to an increase in fresh water consumption and contamination of freshwater resources. One of the major water using operations in industries is the cooling water systems. Cooling water systems use equipments such as cooling towers to remove waste heat from the process to the atmosphere. These systems also generate wastewater through the blowdown mechanisms. Escalating costs of waste treatment, stricter environmental regulations on industrial effluent and scarce water resources have led to studies which concern various means of minimizing water usage and waste generation.
Transfer coefficients are independent of temperature.

\[
\frac{K_a V}{m_w} = c_{pw} \frac{r_{w,\infty}}{T_{w,\infty}} \frac{dT_w}{H_w - H_a}
\]  

(1)

Bernier (1994)[4] further used Merkel’s theory to express \( \frac{K_a V}{m_w} \) as a function of air and water flow rate as shown in Equation (2). This implies that the effect of inlet wet bulb temperature and the inlet water temperature on the coefficient of performance is negligible.

\[
\frac{K_a V}{m_w} = x \left( \frac{m_w}{m_a} \right)^{y}
\]  

(2)

The values of \( x \) and \( y \) parameter can be determined experimentally for a given cooling tower packing. The experimental work completed by the author showed a good approximation of \( \frac{K_a V}{m_w} \). The correlation coefficient for the regression was in magnitude of 0.99.

Kröger (2004)[5] suggested similar correlation for counter flow fills as shown below.

\[
\frac{K_a}{m_w} = \frac{a_d}{A_f} \left( \frac{m_w}{m_a} \right)^{d_w} A T D^{b_d}
\]  

(3)

where \( a_d \), \( d_w \), \( A T D \) and \( b_d \) are system parameters.

Fisenko, et al. (2004)[6] also derived a one dimensional mathematical model for a counter flow mechanical draft cooling tower by solving heat transfer, mass transfer and dynamic equations of a falling water droplet. Equation (4) was used to evaluate the cooling tower efficiency.

\[
\eta = \frac{T_{w,\text{out}} - T_{w,\text{in}}}{T_{w,\text{out}} - T_{w,\text{b}}}
\]  

(4)

Kim and Smith (2001)[7] also developed the cooling tower model which predicts the thermal performance a cooling tower. The authors derived a cooling tower model with the following major assumptions.

- Adiabatic operation in the cooling tower
- Water and dry air flow rate are constant
- Drift and evaporation losses neglected
- Lewis factor is constant

The performance of the cooling tower was assessed by changing the inlet conditions of water and air. The cooling tower performance was then measured by calculating the effectiveness, which is described as the ratio of actual energy transfer to maximum possible energy transfer.


Qureshi and Zubair (2006)[10] developed a cooling tower model which accounts for heat transfer in the spray zone, packing and rain zone. They further developed a fouling model to predict fouling on packing. The mass transfer coefficient was calculated from the same correlation used by Bernier (1994)[4]. Equation (5) was used to evaluate the cooling tower effectiveness. This should not be confused with the cooling tower efficiency by Fisenko et al. (2004)[6].

\[
\varepsilon = \frac{H_{a,\text{out}} - H_{a,\text{in}}}{H_{s,w} - H_{a,\text{in}}}
\]  

(5)

The model used in this manuscript was developed by Kröger (2004)[5] by considering a control volume as shown Figure 2.

![Control volume](image)

The following assumptions were made:

- Interface water temperature is the same as the bulk temperature
- Air and water properties are the same at any horizontal cross section
- Heat and mass transfer area is identical

The governing equations that predict the thermal performance of a cooling tower are given by Equations (6), (7) and (8). Equation (6) and (7) define the mass and energy balance respectively for the control volume. Equation (8) defines the air enthalpy change for the control volume.
\[
\frac{dm_w}{dz} = m_a \frac{dw}{dz} \\
\frac{dT_w}{dz} = \frac{m_a}{cp_w m_w} \left( \frac{dH_a}{dz} - T_w \frac{dw}{dz} \right) \\
\frac{dH_a}{dz} = \frac{K a_f A_{fi}}{m_a} \left( L e_f (H_{ws} - H_a) + (1 - L e_f) H_v (w_i - w) \right)
\]

Where \(a_{fi}\) is the wetted area divided by the corresponding volume of the fill and \(A_{fi}\) is a frontal area. The Lewis factor, \(L e_f\), appearing in Equation (8) is the relationship between the heat-transfer coefficient and the mass-transfer coefficient, i.e. \(\frac{h}{k c_{pma}} = L e\). Lewis factor appears in many governing heat and mass transfer equations. A number of authors like Bernier (1994)[4] and Kim and Smith (2001)[7] assumed the Lewis factor to be unity. Klopper and Kröger (2005)[11] used expression given in Equation (9) to predict the value of Lewis factor. The authors studied the influence of Lewis factor on the performance prediction of wet cooling tower. Their findings were that the influence of Lewis factor diminishes when the inlet ambient air is relatively hot and humid.

\[
L e_f = 0.866^{0.667} \frac{w_s + 0.622}{w + 0.622} - 1 \ln \left( \frac{w_s + 0.622}{w + 0.622} \right)
\]

They further elaborated that increasing Lewis factor increases heat rejection, decreases water outlet temperature and decreases water evaporation rate.

This manuscript presents a technique for grassroot design of cooling water system which incorporates the performances of the cooling towers involved. The study focuses mainly on cooling systems consisting of multiple cooling towers that supply a common set of heat exchangers. The heat exchanger network is synthesized using the mathematical optimization technique. This technique is based on superstructure in which all opportunities for cooling water reuse are explored. The cooling tower model is used to predict the thermal performance of the cooling towers.

![Superstructure for a cooling system](image.png)

Figure 2 Superstructure for a cooling system
The mathematical optimization formulation was developed from the superstructure given in Figure 3 by considering energy and mass balance equations across each cooling water using operation and at each node together with a cooling tower model given above (equations (5) - (9)).

3. Conclusion

The manuscript presents a mathematical technique for cooling water system synthesis with multiple cooling towers. This technique is more holistic because it caters for the effect of cooling tower performance on heat exchanger network. The cooling tower thermal performance is predicted using the mathematical model. The results obtained using this technique are more practical as all components of the cooling water system are embraced. Application of this technique to a case study comprising 3 cooling towers and 6 heat exchangers demonstrated that it can result in more than 17% reduction in circulating water with significant savings in associated make-up and blowdown water.

References